

ECE/ENGRD 2100

Introduction to Circuits for ECE

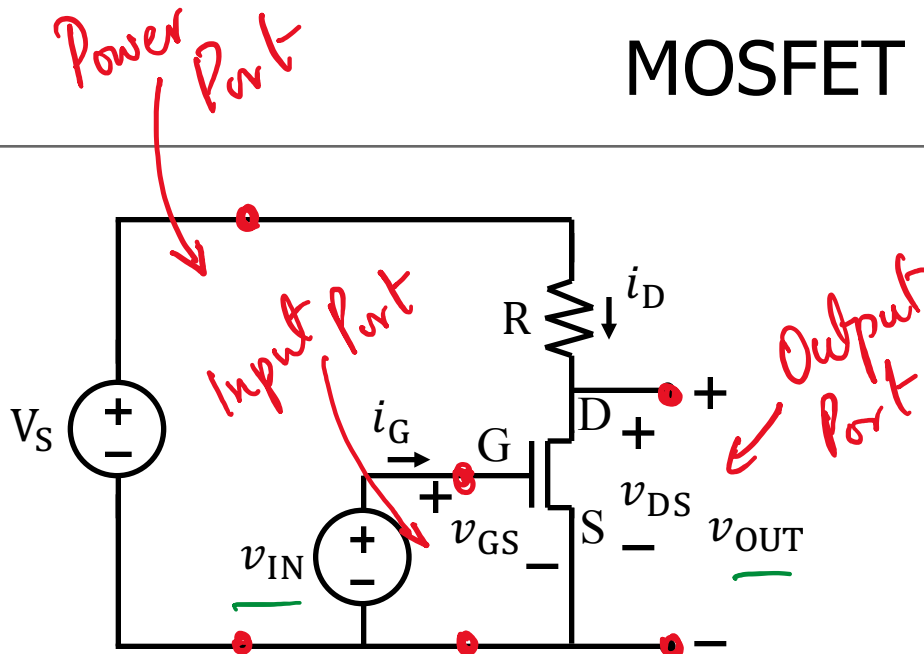
Lecture 13

Op-Amps and Op-Amp Amplifiers

Announcements

- Recommended Reading:
 - Textbook Chapter 5
- Upcoming due dates:
 - Lab report 2 due by 11:59 pm on Wednesday 27, 2019
- Prelim 1 on **Thursday February 21**, 2019 from **7:30 – 9 pm in 203 Phillips**
 - Email afridi@cornell.edu if have conflict
 - Make up exams on same day (Thursday February 21):
 - **10 – 11:30 am in 307 Phillips**
 - **2:30 – 4 pm in 310 Rhodes** (room has changed)
 - Will cover material through Lecture 11
 - Prelim is closed-book and closed-notes
 - One double-sided page formula sheet is allowed
 - Bring a calculator

MOSFET Amplifier



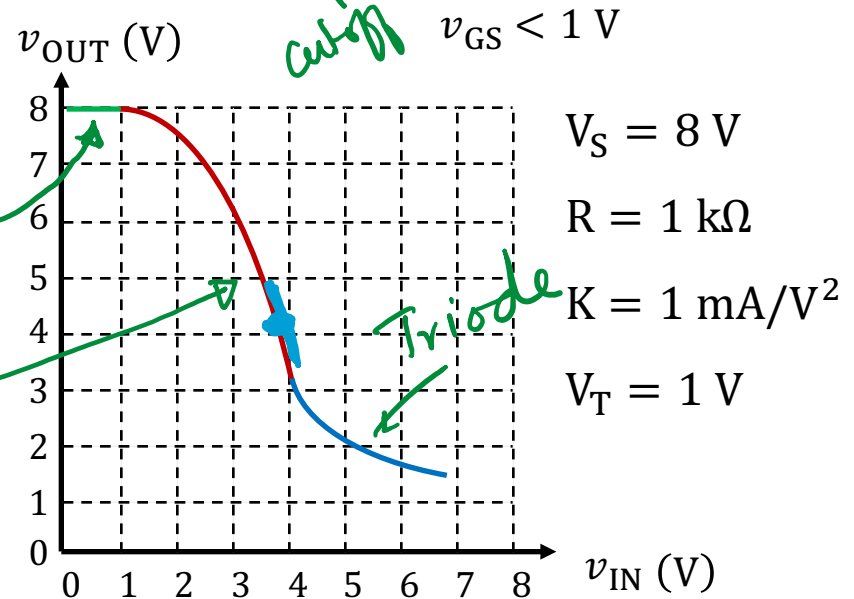
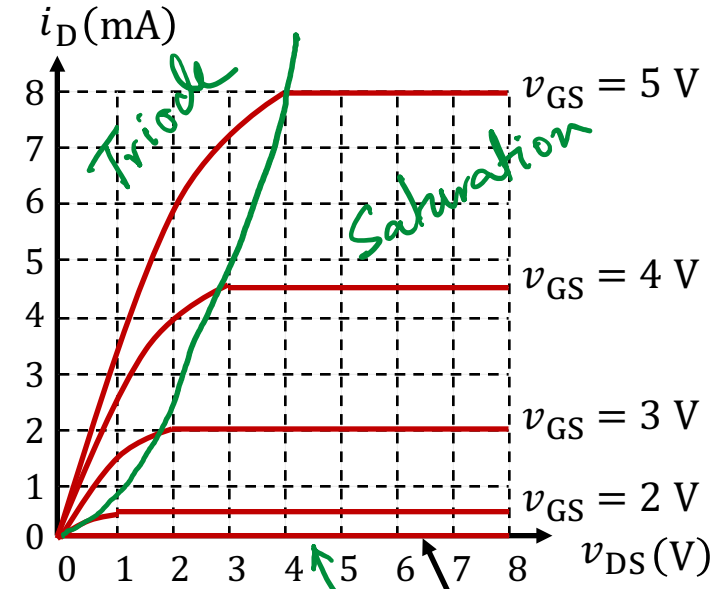
Large-Signal Response

$$v_{OUT} = V_S - \frac{RK}{2} (v_{IN} - V_T)^2$$

Small-Signal Response

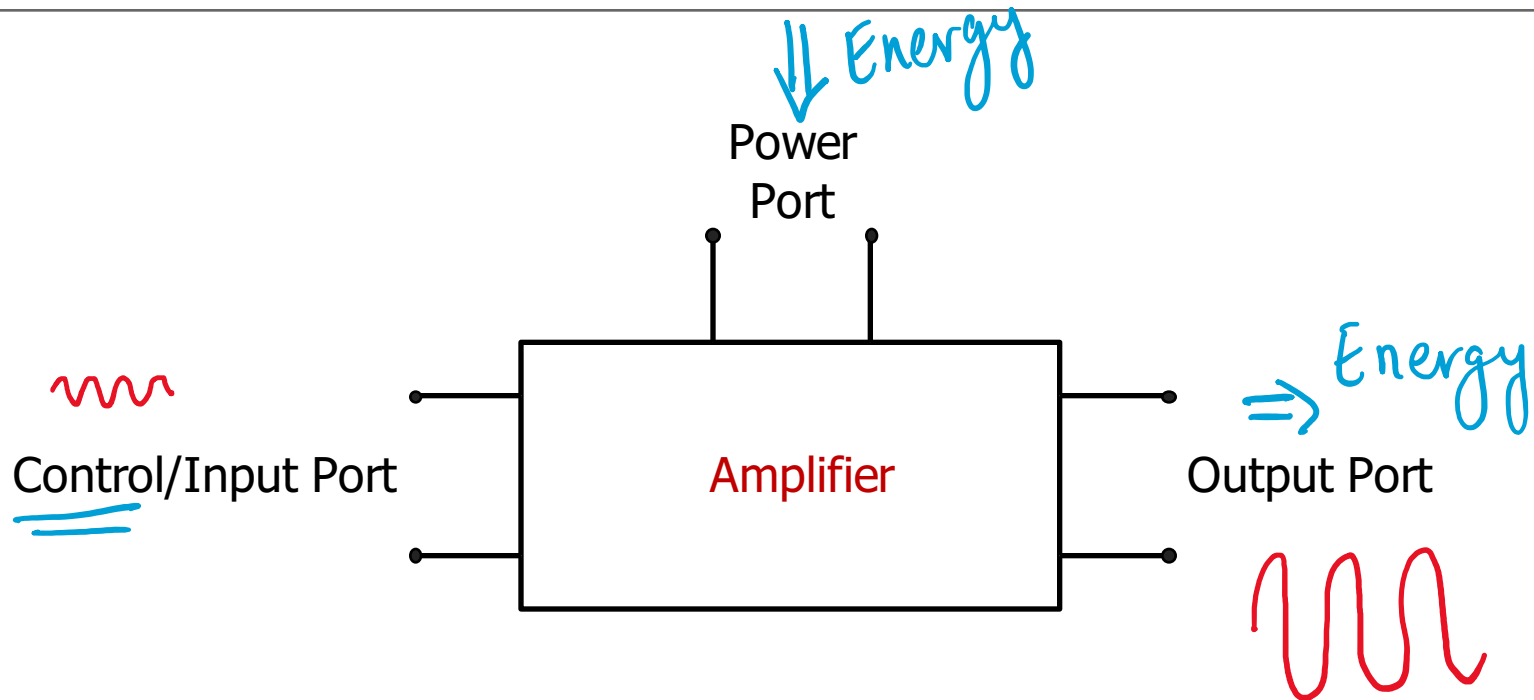
$$v_{out} = \underbrace{-RK}_{1} \underbrace{(V_{IN} - V_T)}_{3} \cdot v_{in}$$

Saturation



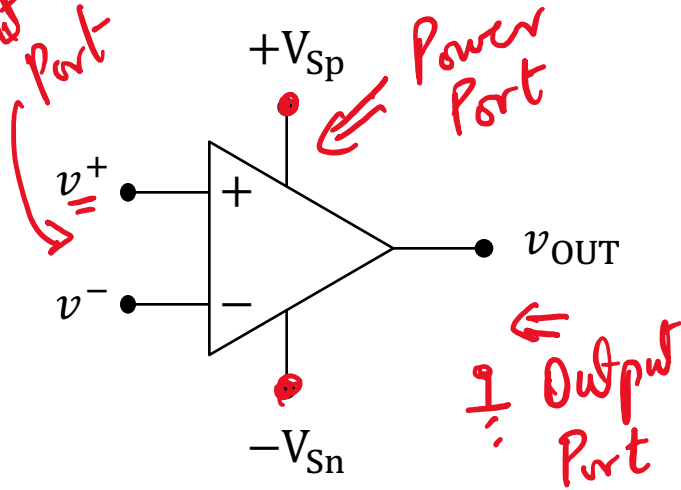
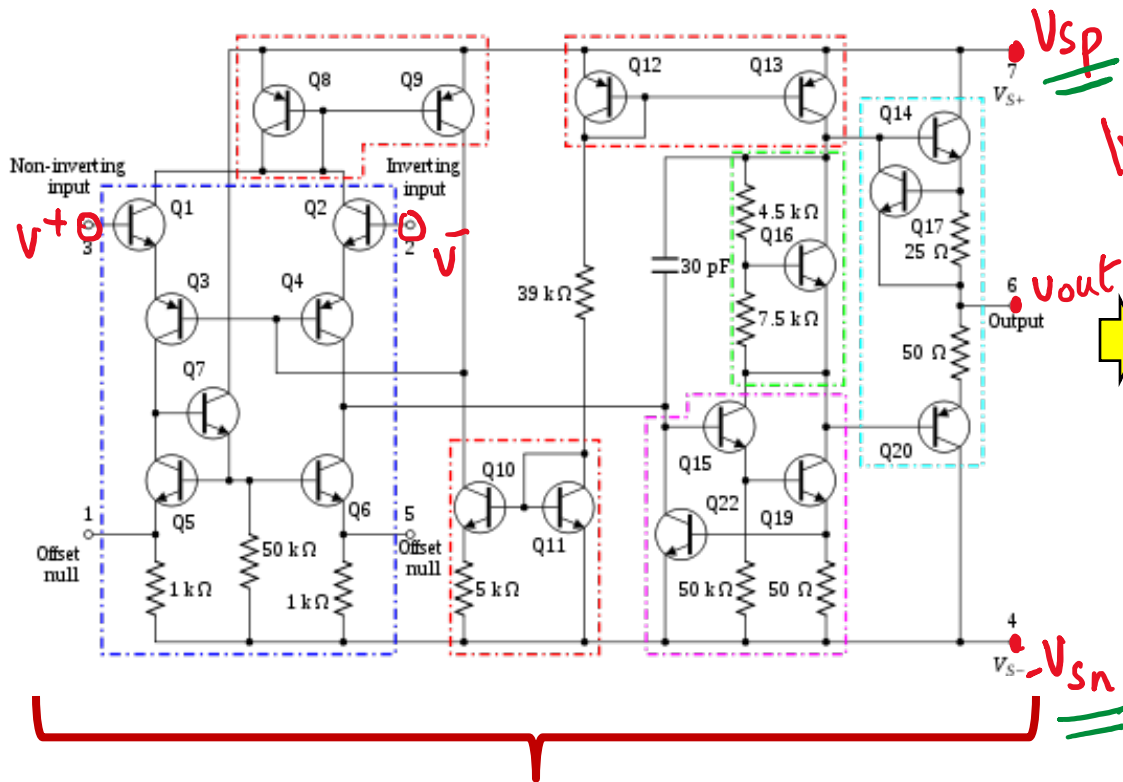
Cutoff
Saturation

Amplifiers

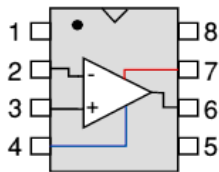


- Amplifier is a three port device
- Provides power gain (voltage gain, current gain or both)
- Fundamental building block in analog signal processing systems, such as audio and video communications, instrumentation and control, etc.

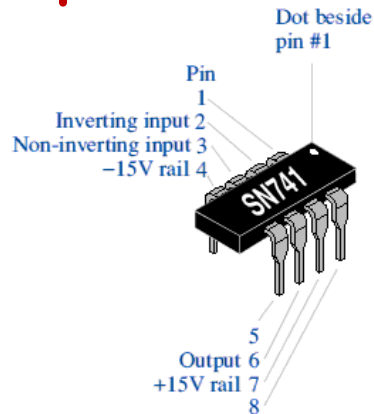
Operational Amplifier (Op-Amp)



741 Op Amp
8-pin DIP



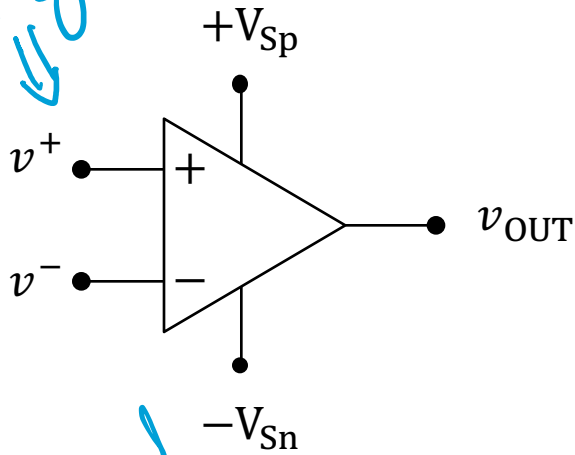
Top view



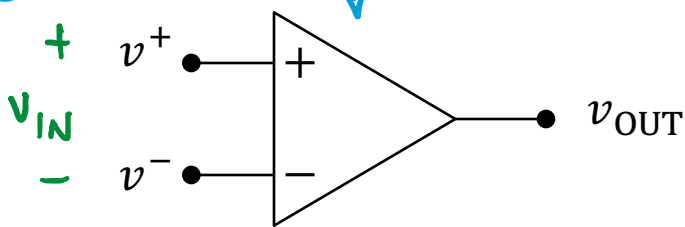
741 Op Amp

Simple Op-Amp Model

Full Symbol



Short-hand notation



Typically do not show power supply terminals

$$v_{OUT} = A(v^+ - v^-)$$

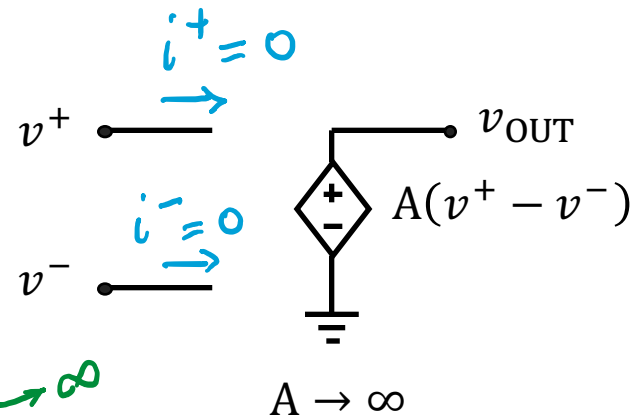
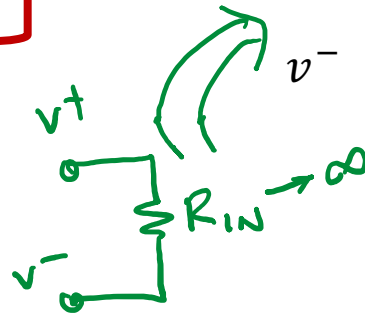
$$\underline{v_{OUT} = A v_{IN}}$$

Ideal Op Amp has:

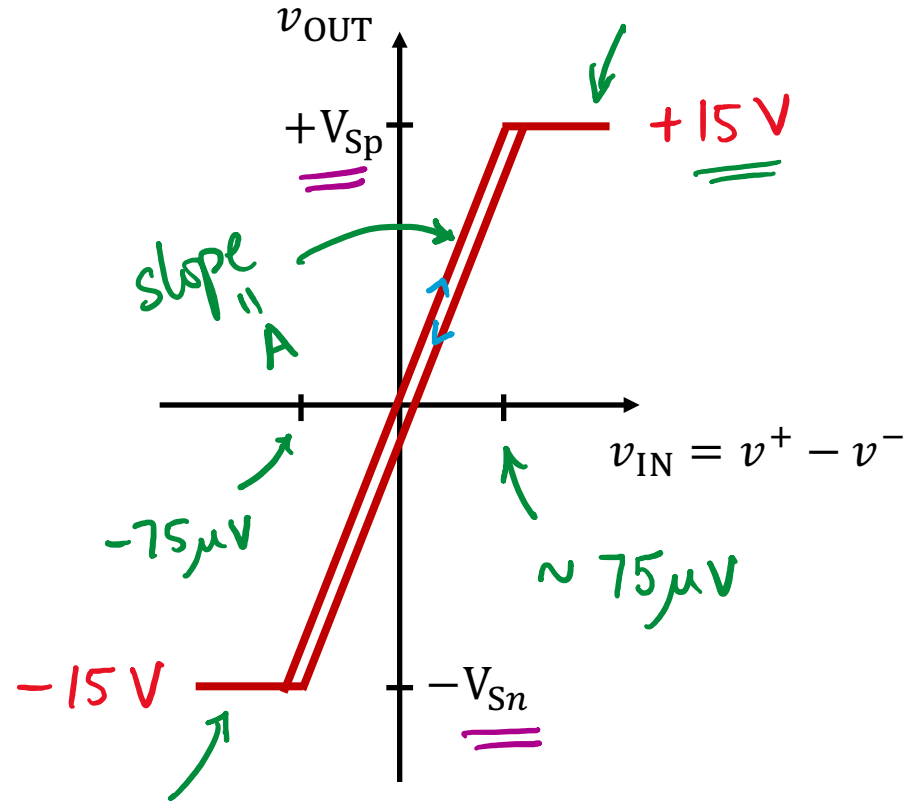
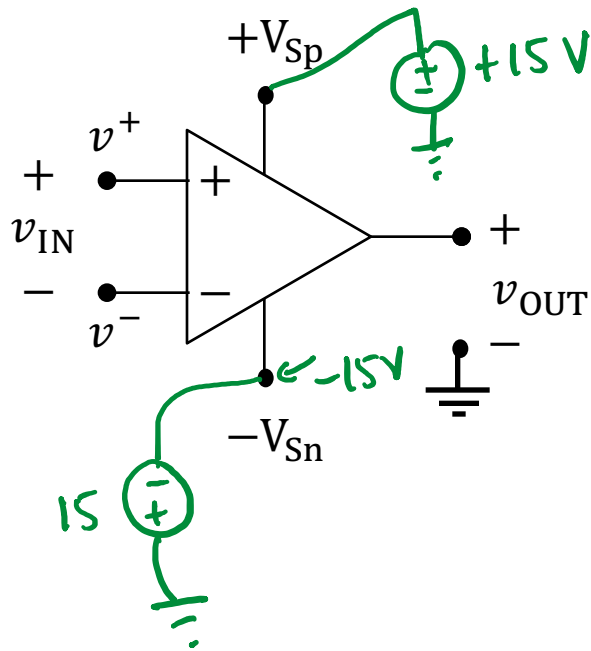
Infinite Gain, i.e., $A \rightarrow \infty$

Infinite Input Resistance \leftarrow

Output v_{OUT} can take any value \leftarrow



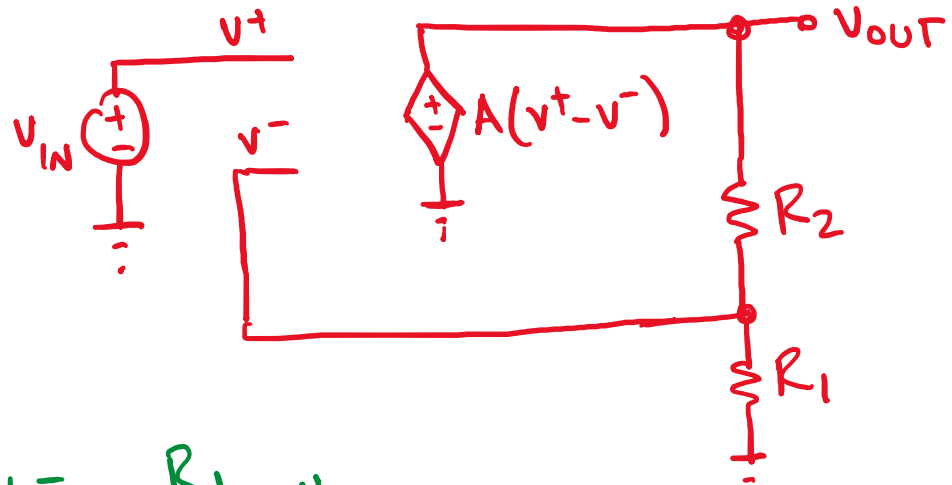
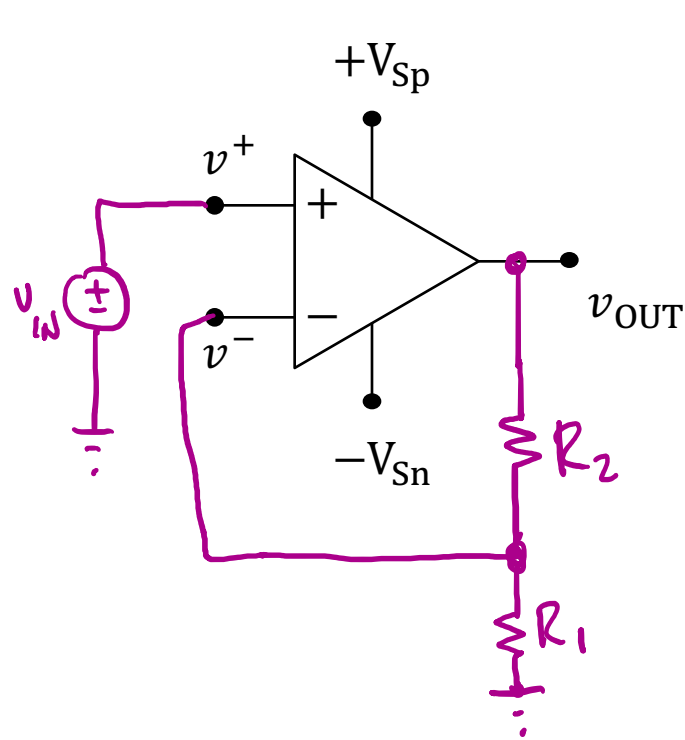
Real Op-Amp Behavior



- Voltage gain, $A \equiv \frac{v_{OUT}}{v_{IN}} \approx 200,000$
- Non-linear
- Temperature dependent

} Non-idealities

Practical Amplifier Design



$$v^- = \frac{R_1}{R_1 + R_2} v_{OUT}$$

$$v_{OUT} = A(v^+ - v^-) = A\left(v_{IN} - \frac{R_1}{R_1 + R_2} v_{OUT}\right)$$

$$\Rightarrow v_{OUT} \left(1 + \frac{R_1 A}{R_1 + R_2}\right) = A v_{IN} \Rightarrow v_{OUT} = \frac{A v_{IN}}{1 + \frac{R_1 A}{R_1 + R_2}} \quad \left(1 + \frac{R_2}{R_1}\right) v_{IN}$$

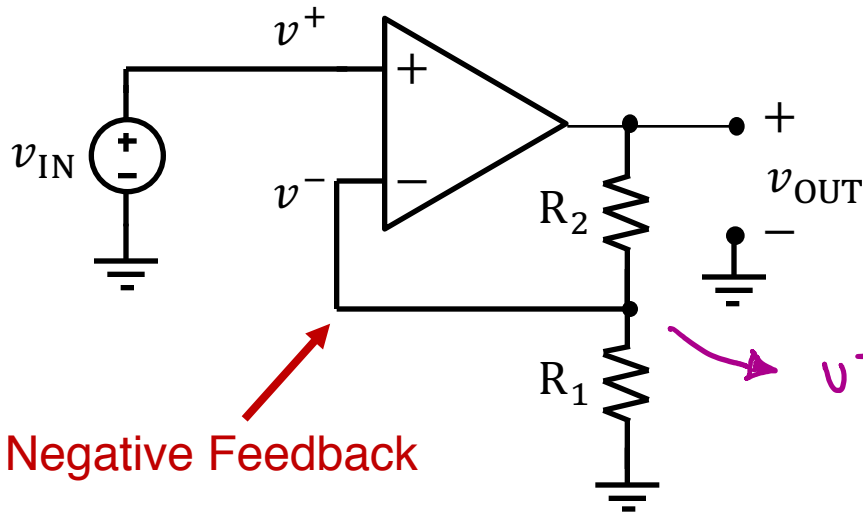
$$\Rightarrow v_{OUT} = \frac{v_{IN}}{\frac{1}{A} + \frac{R_1}{R_1 + R_2}}$$

Use A is very large
 $A \gg \frac{R_1 + R_2}{R_1}$

$$\Rightarrow v_{OUT} = \frac{R_1 + R_2}{R_1} v_{IN}$$

new gain \uparrow

Non-Inverting Amplifier



$$v_{OUT} = \frac{v_{IN}}{\frac{1}{A} + \frac{R_1}{R_1 + R_2}}$$

$$\Rightarrow v^- = \frac{R_1}{R_1 + R_2} v_{OUT} = \frac{\frac{R_1}{R_1 + R_2}}{\frac{1}{A} + \frac{R_1}{R_1 + R_2}} \cdot v_{IN}$$

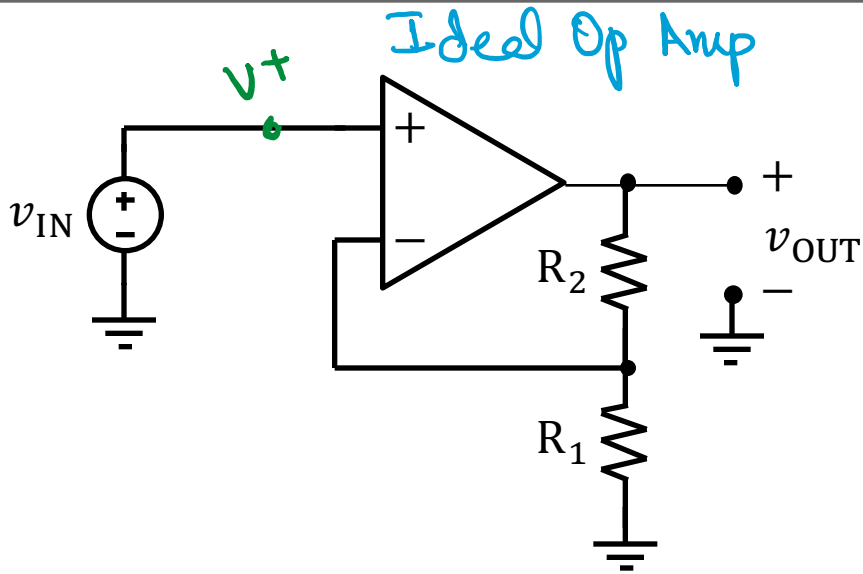
$$\Rightarrow \underline{v^- = v_{IN}} \quad \text{as } A \rightarrow \infty$$

$$v^+ = v_{IN}$$

$$\boxed{v^- = v^+} \quad \text{as } A \rightarrow \infty$$

$v^- \approx v^+$ under negative feedback & very large A

Shortcut Analysis of Op Amps with Negative Feedback



Non-Inverting
Amplifier

Under negative feedback

$$v^- \approx v^+$$

$$v^+ = v_{IN} \Rightarrow v^- \approx v_{IN}$$

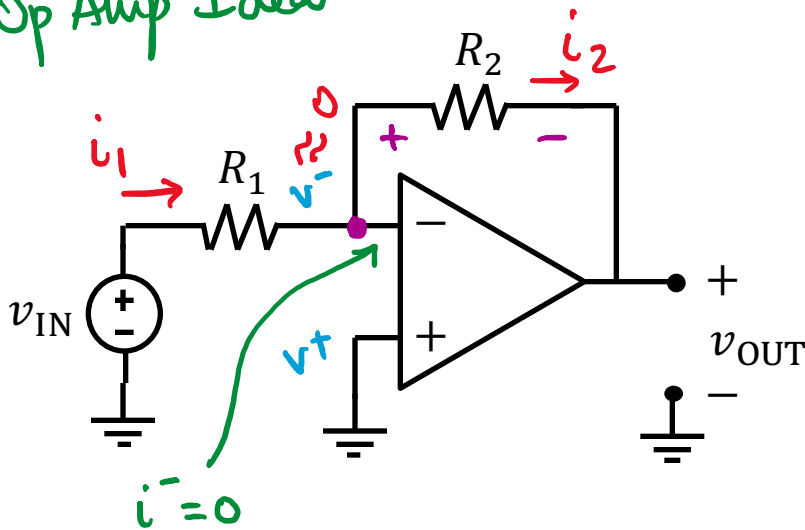
$$v^- = \frac{R_1}{R_1 + R_2} v_{OUT} = v_{IN}$$

$$\Rightarrow v_{OUT} = \frac{R_1 + R_2}{R_1} v_{IN}$$

Same as before

Inverting Amplifier

Op Amp Ideal



Have negative feedback

$$v^- \approx v^+$$

$$v^- \approx 0V$$

$$i_1 = \frac{v_{IN}}{R_1}$$

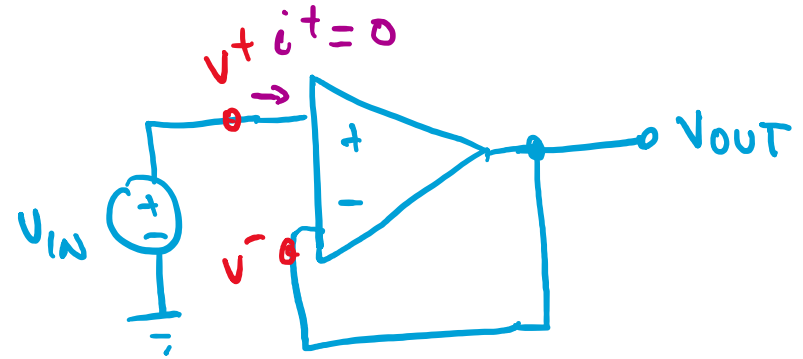
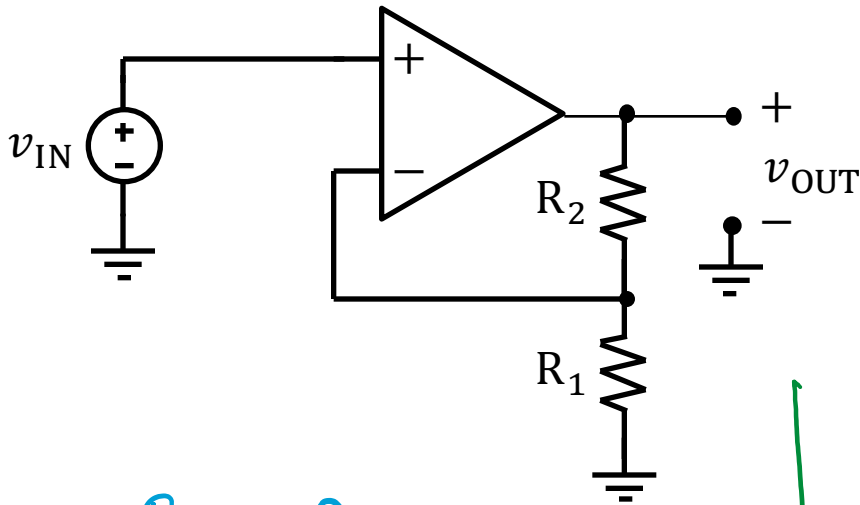
$$i_2 = i_1 = \frac{v_{IN}}{R_1}$$

$$v_{OUT} = 0 - R_2 i_2 \Rightarrow$$

$$v_{OUT} = -\frac{R_2}{R_1} v_{IN}$$

Inverting Amplifier

Voltage Buffer



$$R_2 = 0$$

$$R_1 \rightarrow \infty$$

$$\begin{aligned} v_{OUT} &= \frac{R_1 + R_2}{R_1} v_{IN} \\ &= \left(1 + \frac{R_2}{R_1}\right) v_{IN} = v_{IN} \end{aligned}$$

Negative Feedback

$$v^- = v_{OUT}$$

$$v^- \approx v^+ = v_{IN}$$

$$\Rightarrow v_{OUT} = v_{IN}$$