Department of Electrical and Computer Engineering, Cornell University

## **ECE 3150: Microelectronics**

## Spring 2016

Homework 7

Due on March. 17, 2016 at 7:00 PM

## Suggested Readings:

a) Lecture notes

#### **Important Notes:**

 MAKE SURE THAT YOU INDICATE THE UNITS ASSOCIATED WITH YOUR NUMERICAL ANSWERS. OTHERWISE NO POINTS WILL BE AWARDED.
 Unless noted otherwise, always assume room temperature.
 Midterm on March 24, 7:30-10:00 PM in KMBB11.

# Problem 7.1: (A Simple NFET Amplifier)

Consider the following NFET amplifier:



For the NFET assume:

$$W = 10 \ \mu m$$
  

$$L = 1 \ \mu m$$
  

$$\mu_n C_{ox} = 200 \ \mu A / V^2$$
  

$$\lambda_n = 0.1 \ 1 / V$$
  

$$V_{DD} = 2.5 \ V$$
  

$$R_L = 10 \ k\Omega$$
  

$$V_{TN} = 0.5 \ V$$
  

$$N_a = 10^{17} \ cm^{-3}$$

In the following parts, assume that the load resistor  $R_L$  is NOT connected to the output.

a) Generally one would like to keep the resistor R large. But if it is too large, the FET could go into the linear region for a given desired value of the DC drain current  $I_D$ . Suppose you are at liberty to choose any value of the DC input bias voltage  $V_{IN}$ . For every value of  $V_{IN}$  above  $V_{TN}$  the value of the resistor R has to be within a range in order to keep the FET in the saturation region of operation. For values of  $V_{IN}$  between 0.5 and 2.5 Volts, find the maximum ( $R_{max}$ ) and the minimum ( $R_{min}$ ) values of the resistance R needed to keep the FET working the saturation region. Plot  $R_{max}$  and  $R_{min}$  on the same plot as a function of  $V_{IN}$ .

b) Suppose you need to the keep the DC voltage at the output  $V_{OUT}$  equal to 1.5 V. And you also need to keep the small signal gain, and therefore  $g_m$ , reasonably high, so you choose  $I_D = 200 \ \mu A$ . What should be the values of the resistor R and the input bias voltage  $V_{IN}$  needed to meet these objectives? Or can these objectives even be met while keeping the FET in the saturation region?

c) With the numerical value of the resistor as in part (b), and a varying input voltage  $V_{IN}$ , what are the maximum and the minimum values of the ouput voltage  $V_{OUT}$  such that the FET remains in the saturation region?

d) With the value of the resistor as in part (b), what are the maximum and the minimum values of the input voltage  $V_{IN}$  such that the FET remains in the saturation region?

e) With the value of the resistor as in part (b), compute and plot (sketches not acceptable) the transfer curve  $V_{OUT} - vs - V_{IN}$  and indicate regions in which the FET is in the cut off, linear, and saturation regions.

f) With the value of the resistor and the biasing scheme as in part (b), what is the open circuit small signal voltage gain  $A_V = v_{out}/v_{in}$  (i.e. the voltage gain with the load resistor disconnected)? Need a numerical number as an answer and not just a formula.

Now suppose the load resistor  $R_L$  is connected to the output of the amplifier. Its presence will change things significantly.

g) Suppose your biasing scheme, including values of  $V_{IN}$  and R are as in part (b) above. With the load resistor now connected, what is the new output voltage  $V_{OUT}$ ? Hint: it is not going to be 1.5 Volts anymore. And what is  $I_{OUT}$ ? Lesson: loading can affect the DC biasing of an amplifier!

h) Suppose your biasing scheme, including values of  $V_{IN}$  and R are as in part (b) above. With the load resistor now connected, what is the small signal voltage gain  $A_V = v_{out}/v_{in}$ ? Need a numerical number as an answer and not just a formula. Has it decreased or increased compared to the case when the load resistor was not connected?

Lesson: loading can affect the small signal performance of an amplifier!

### Problem 7.2: (NFET Loaded NFET Amplifier)

Consider the following circuit:



Assume that for both NFETs:

$$W = 10 \ \mu m$$

$$L = 1 \ \mu m$$

$$\mu_n C_{ox} = 200 \ \mu A / V^2$$

$$\lambda_n = 0.11 / V$$

$$V_{DD} = 2.5 \ V$$

$$V_{TN} = 0.5 \ V$$

$$N_a = 10^{17} \ cm^{-3}$$

a) If  $V_{IN} = 1.25$  V, find  $V_{OUT}$ ? Is the bottom NFET in linear or saturation region?

b) If  $V_{IN} = 2.0 \text{ V}$ , find  $V_{OUT}$ ? Is the bottom NFET in linear or saturation region?

c) What is the highest voltage  $V_{OUT}$  can take if both the FETs are to remain in saturation? What is the corresponding input voltage  $V_{IN}$ ?

d) What is the lowest voltage  $V_{OUT}$  can take if both the FETs are to remain in saturation? What is the corresponding input voltage  $V_{IN}$ ?

e) Draw a small signal circuit for the amplifier and find an expression for the open circuit voltage gain  $A_v = v_{out}/v_{in}$ .

f) Suppose  $V_{IN} = 1.25$  V. Find the values of  $g_{m1}$ ,  $g_{m2}$ ,  $r_{o1}$ ,  $r_{o2}$  for the two NFETs and then find the value of the voltage gain  $A_v = v_{out}/v_{in}$  at this bias point.

# Problem 7.3: (PFET Loaded NFET Amplifier)

Consider the following circuit:



a) If  $V_B = 1.25$  V, and  $V_{IN} = 1.25$  V, what is  $V_{OUT}$ ?

b) If  $V_B = 1.25$  V, what is the highest voltage  $V_{OUT}$  can take if both the FETs are to remain in saturation? What is the corresponding input voltage  $V_{IN}$ ?

c) If  $V_B = 1.25$  V, what is the lowest voltage  $V_{OUT}$  can take if both the FETs are to remain in saturation? What is the corresponding input voltage  $V_{IN}$ ?

d) Draw a small signal circuit for the amplifier and find an expression for the open circuit voltage gain  $A_V = v_{out}/v_{in}$ .

e) If  $V_B = 1.25$  V, and  $V_{IN} = 1.25$  V, find the values of  $g_{m1}$ ,  $g_{m2}$ ,  $r_{o1}$ ,  $r_{o2}$  for the two FETs and then find the value of the voltage gain  $A_v = v_{out}/v_{in}$  at this bias point.

f) Based on what you have found, would you use the amplifier of problem 7.1(f), problem 7.2(f) or the amplifier of this problem 7.3(e) for high gain applications?